

Three-Centre Cluster Structure in ^{11}C and ^{11}B

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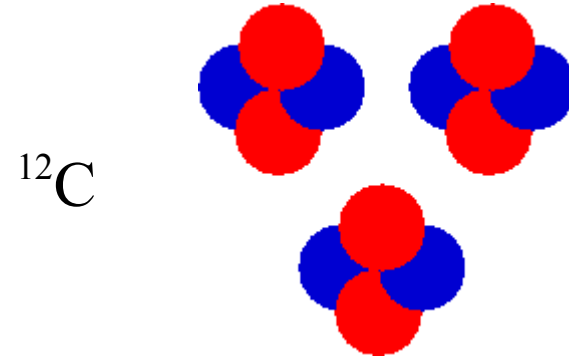
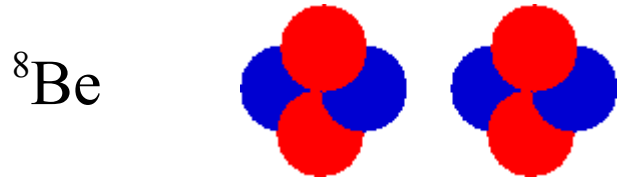
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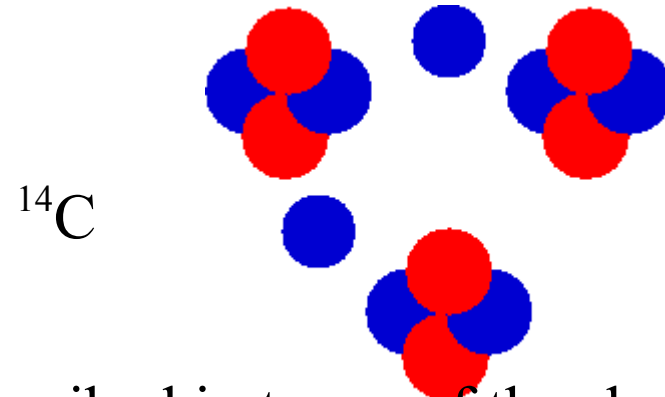
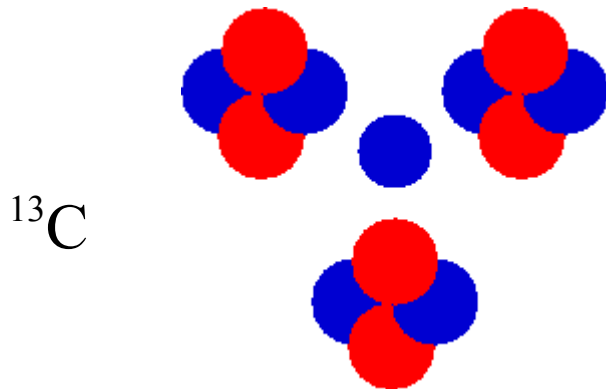
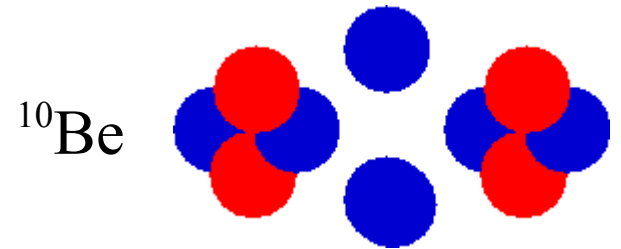
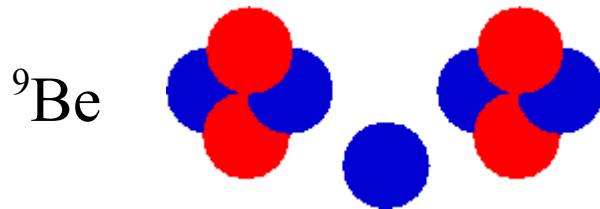
NUSTAR'05, University of Surrey,
Guildford, Jan 2005.

INTRODUCTION

- many light nuclei possess a prominent **cluster structure**
- α -particle: basic unit in cluster structures

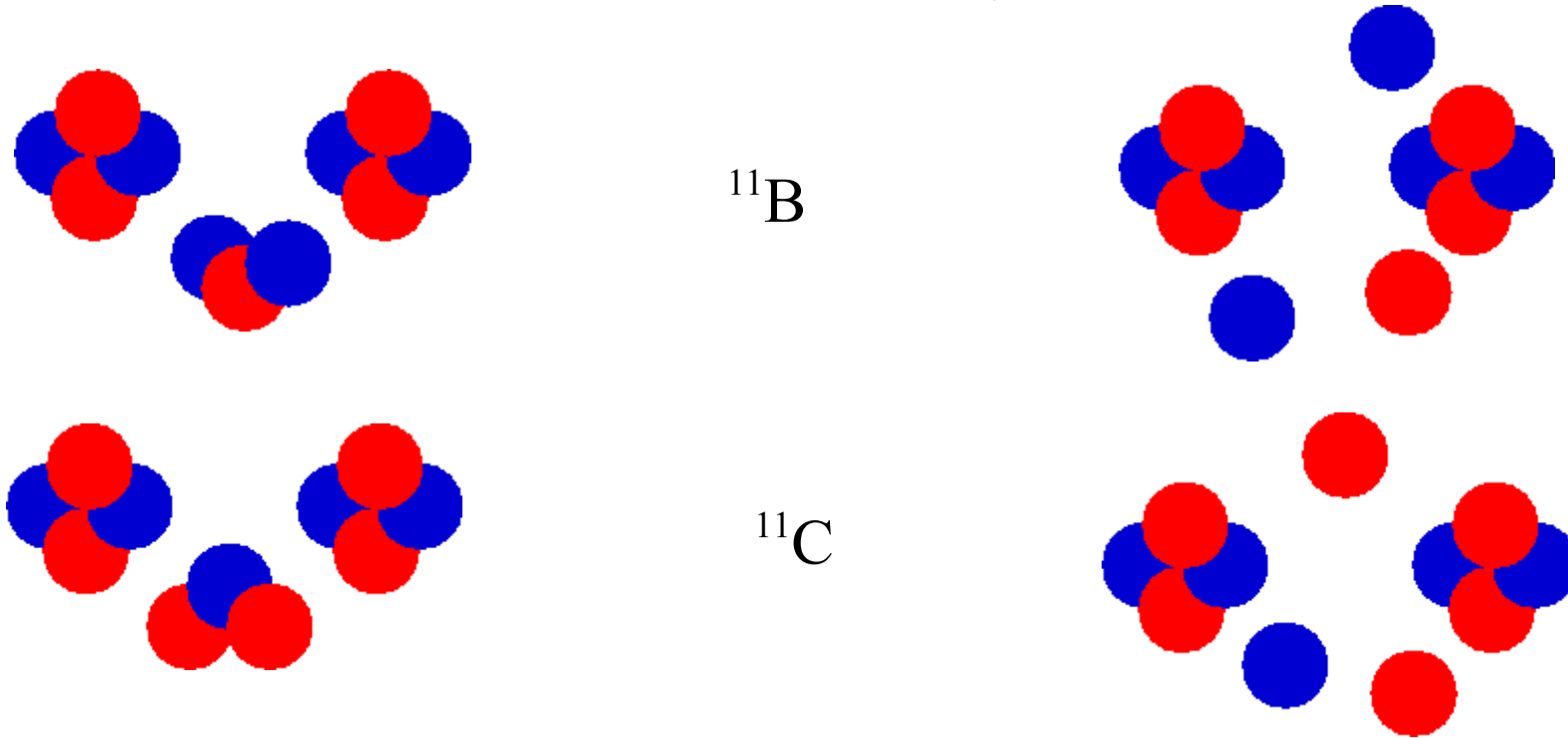


- attention has focused on neutron-rich Be and C nuclei: $N\alpha+Mn$ structure



- properties of Be and C nuclei may be described in terms of the sharing of the valence neutrons between the α -cores – **nuclear molecules**

- interesting issue: influence of α -clustering on the structure of neutron deficient ^{11}C and also on boron isotopes, particularly ^{11}B
- are these mirror nuclei two- or three-centre systems ?



- example of the 3-centre systems where are holes rather than particles being exchanged between α -particles

- knowledge of their structure may help in understanding of the molecular nature of light nuclei and its evolution from 2- to 3-centre structure

- **astrophysical interest:** $^7\text{Be}(\alpha,\gamma)^{11}\text{C}$ reaction is starting point of the hot pp chain and $^7\text{Li}(\alpha,\gamma)^{11}\text{B}$ may bypass $A=8$ gap in the big-bang nucleosynthesis

- **experimental signatures** for excited states with developed cluster structure:
 - a) reaction mechanism by which the states are populated
 - b) large population/decay probability for the channel associated with cluster structure and suppressed single-nucleon population/decay probability
 - c) rotational band associated with large deformation (moment of inertia I)

$$E_{exc} \sim \frac{\hbar^2}{2I} * [J(J+1)]$$

- d) strong γ -transitions between states in the rotational band

- **^{11}C** and **^{11}B** have been studied extensively but the experimental evidence for cluster structures is rather scarce
- here presented the results of experimental studies which probe cluster structure of **^{11}C** and **^{11}B** via the α -decay of their excited states
- **^{11}C states**: the $^{16}\text{O}(^9\text{Be}, \alpha ^7\text{Be})^{14}\text{C}$ reaction
- **^{11}B states**: the $^7\text{Li}(^9\text{Be}, \alpha ^7\text{Li})^5\text{He}$ and $^7\text{Li}(^9\text{Be}, \alpha \alpha t)^5\text{He}$ reactions
- resonant particle spectroscopy technique
- two-nucleon transfer processes onto the $2\alpha+n$ cluster nucleus ^9Be provide a mechanism by which the multi-centre cluster structures may be populated

EXPERIMENTAL DETAILS

-measurements performed at the Australian National University's 14UD tandem accelerator facility, Canberra, Australia

- beam: 70 and 55 MeV ^9Be , intensity ~ 3 enA

- target: Li_2O_3 foil,
 $100 \mu\text{g}/\text{cm}^2$

- detector array:
four telescopes for
charged particles in a
cross-like arrangement

T1: $17.3^\circ \phi=0^\circ$

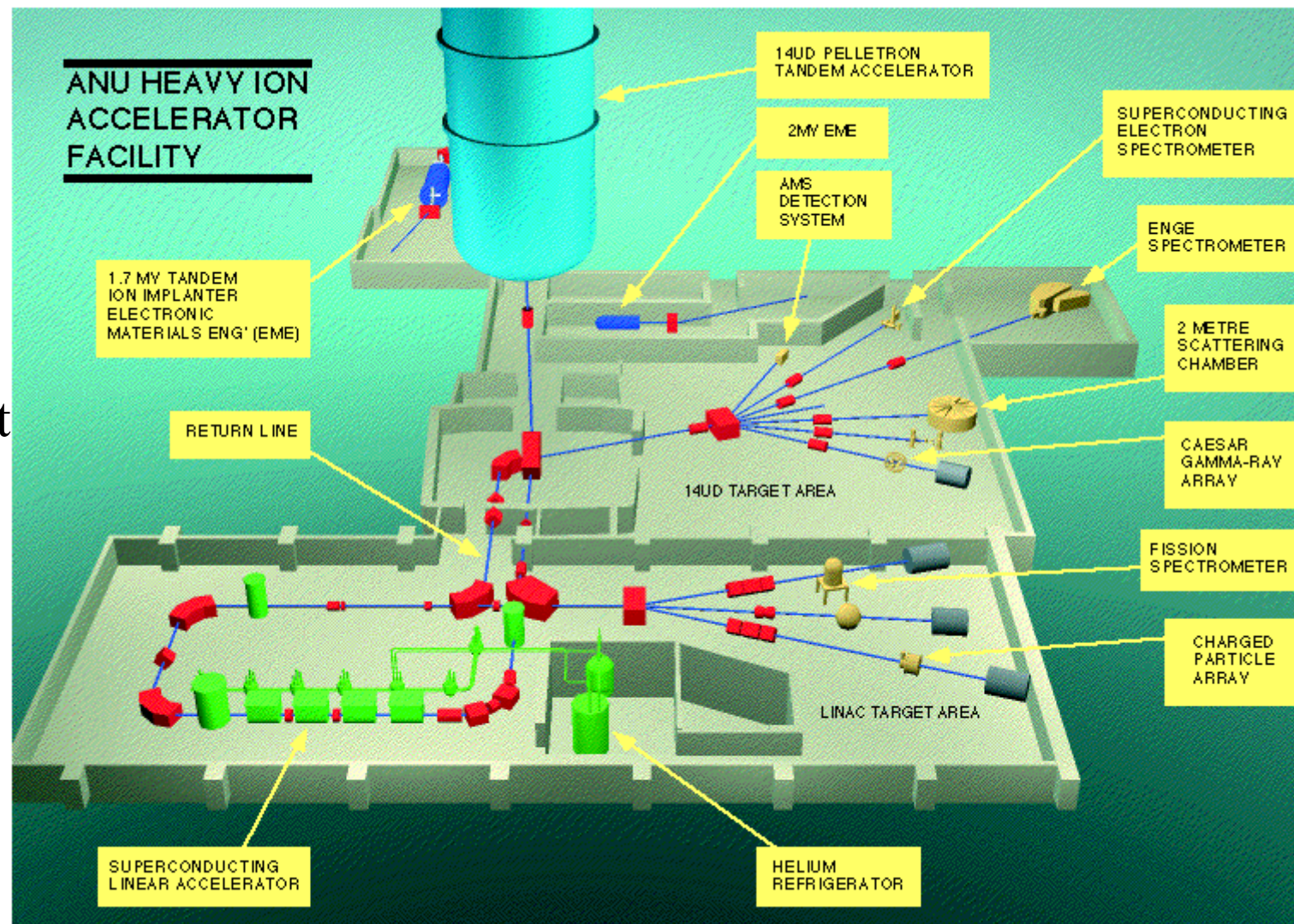
T2: $17.8^\circ \phi=180^\circ$

$\Theta = \sim 7^\circ - \sim 28^\circ$

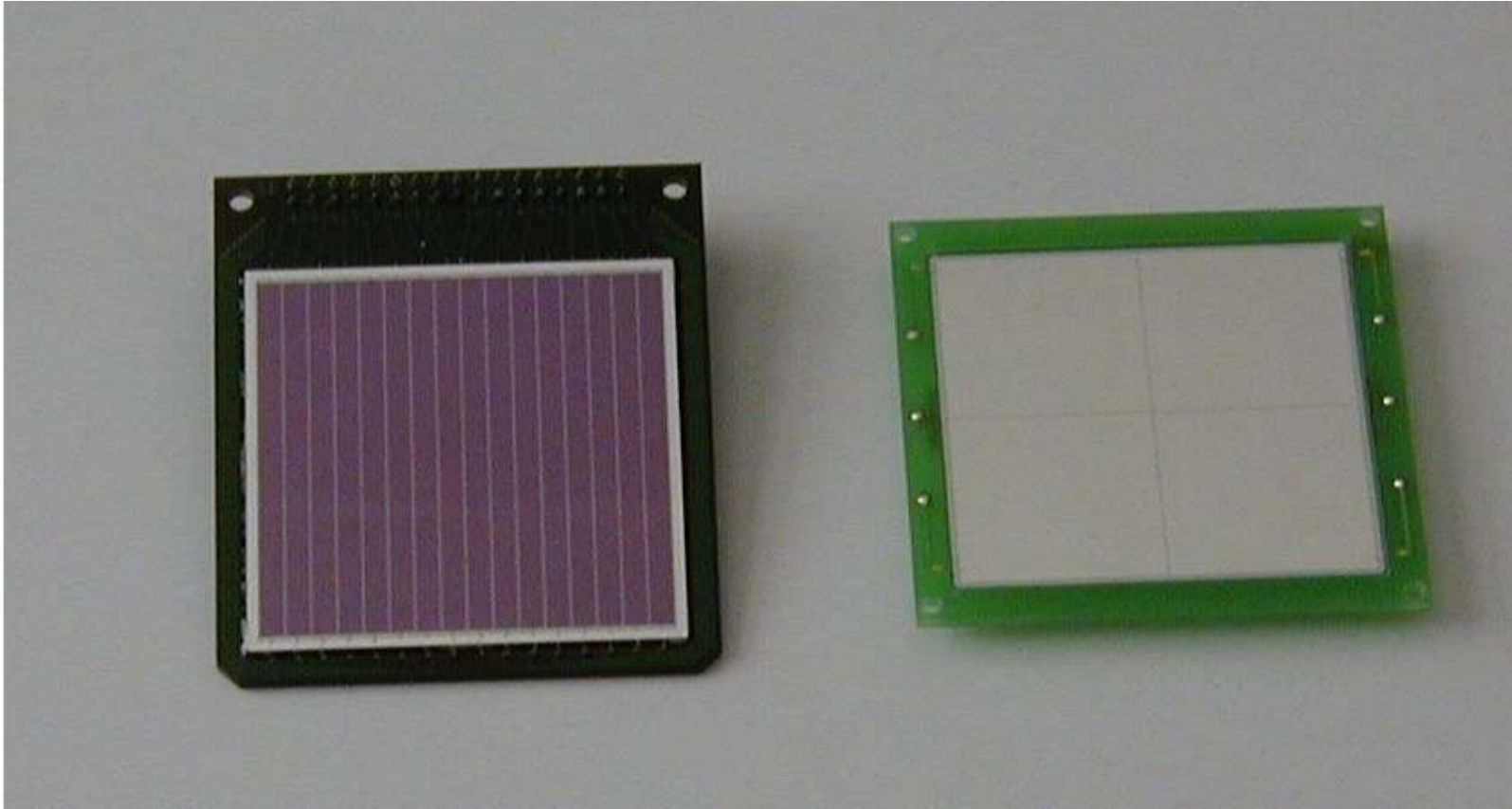
T3: $28.6^\circ \phi=90^\circ$

T4: $29.7^\circ \phi=270^\circ$

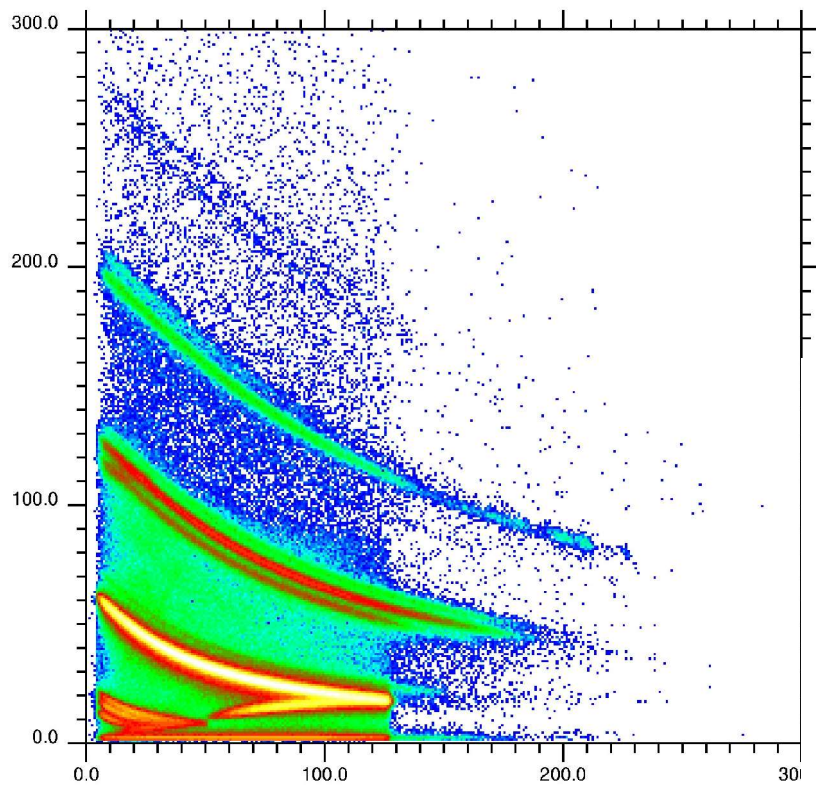
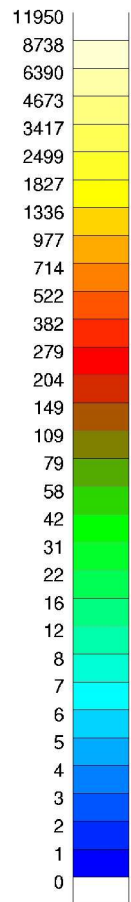
$\Theta = \sim 20^\circ - \sim 38^\circ$



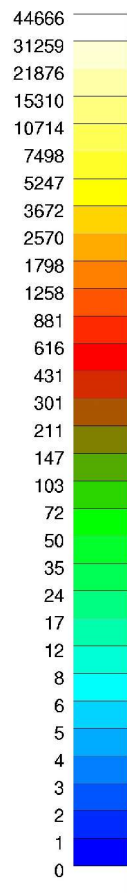
- telescopes contained 3 elements: $70\ \mu\text{m}$ $5\times 5\ \text{cm}^2$ silicon detectors segmented into four squares, $500\ \mu\text{m}$ $5\times 5\ \text{cm}^2$ silicon strip detectors divided into 16 position-sensitive strips, 2.5 cm thick CsI detectors



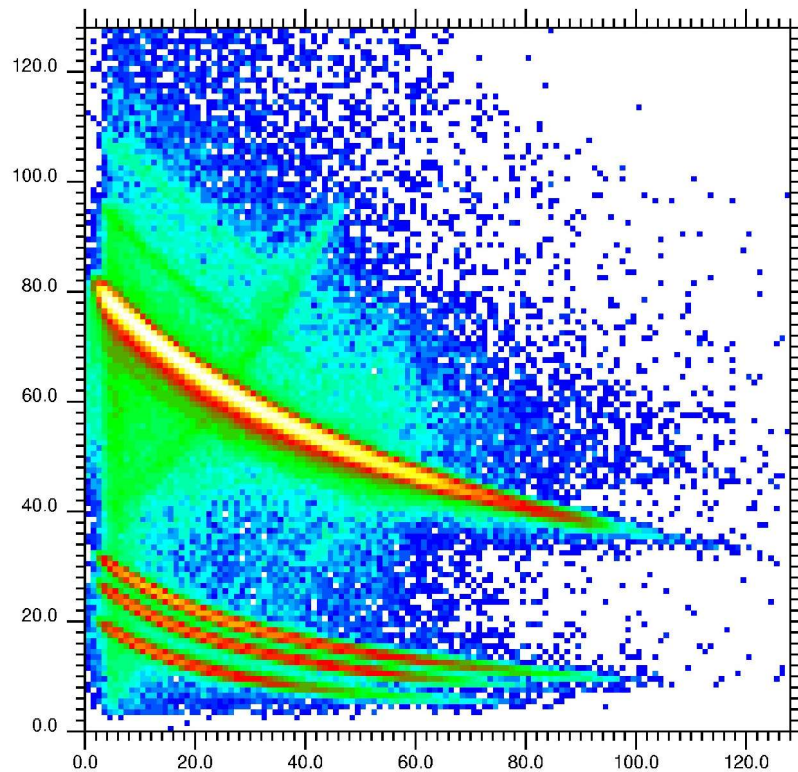
- charge and mass resolution from hydrogen to beryllium isotopes
- kinematically complete measurements of the reactions with 3 and 4 particles in the exit channel: determination of the momentum of each particle in the coincident events
- the reaction kinematics fully reconstructed



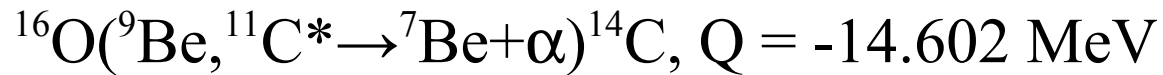
Si – Si matrix



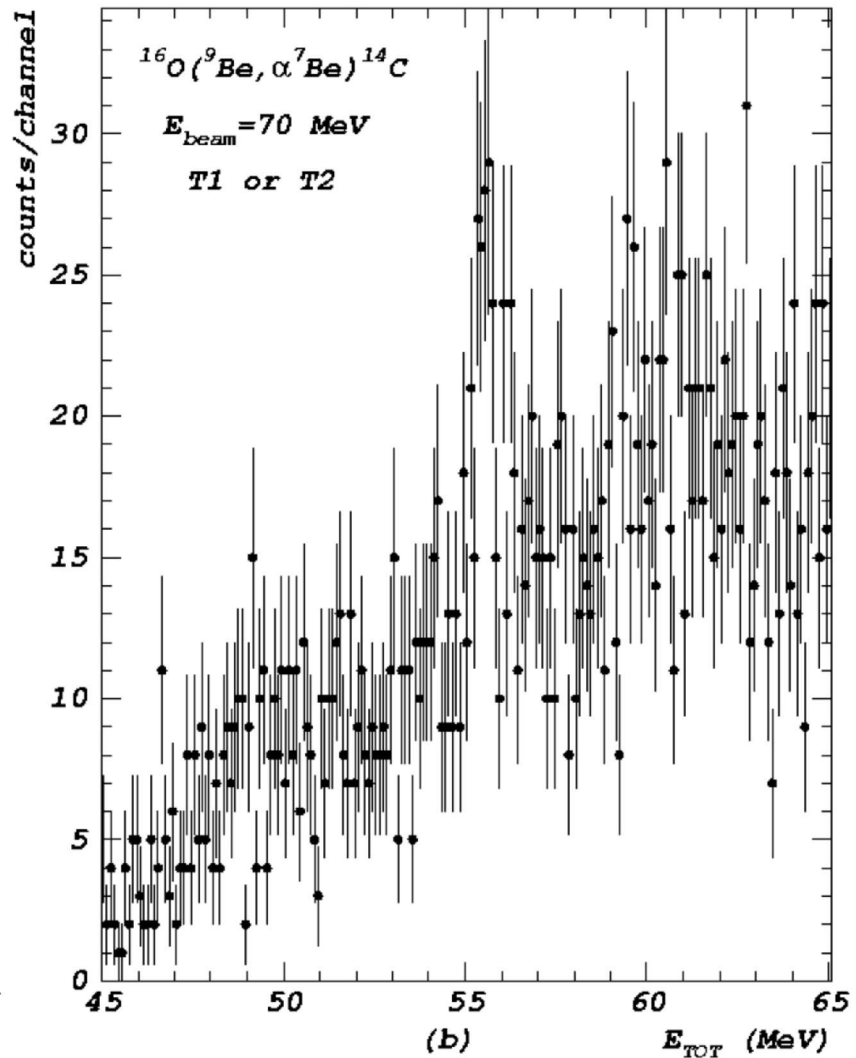
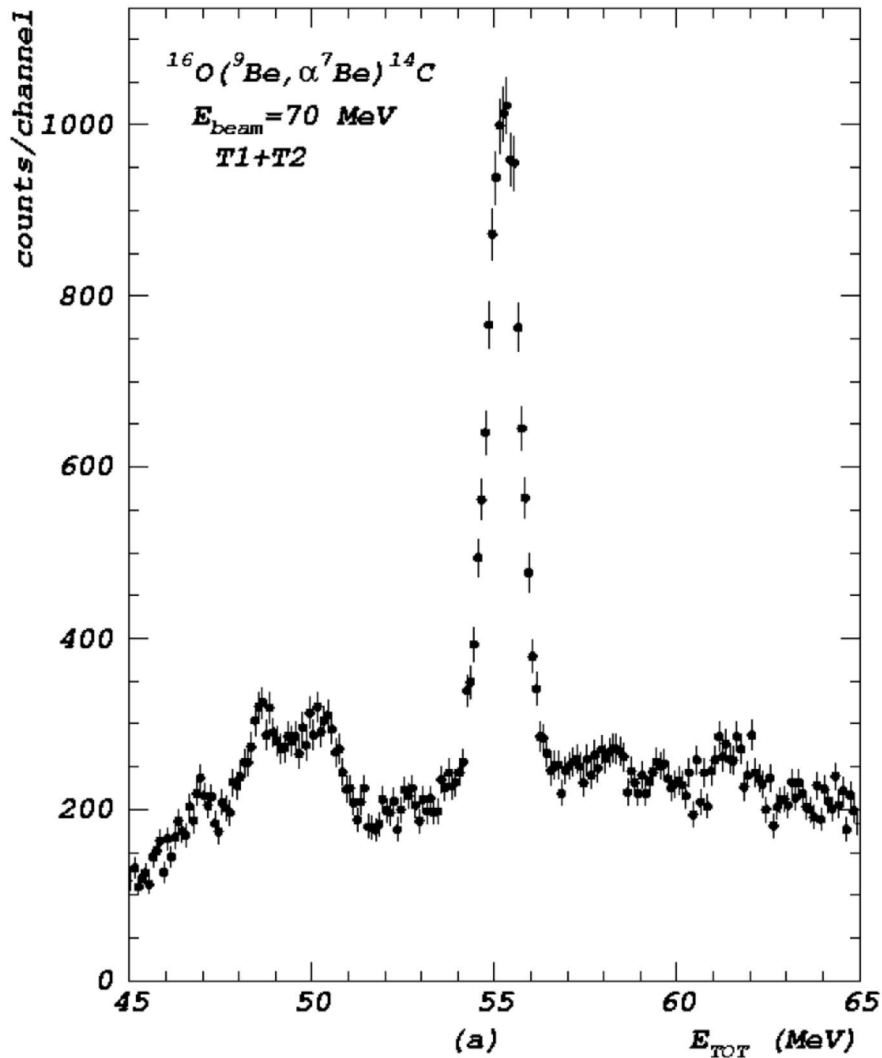
Si – CsI matrix



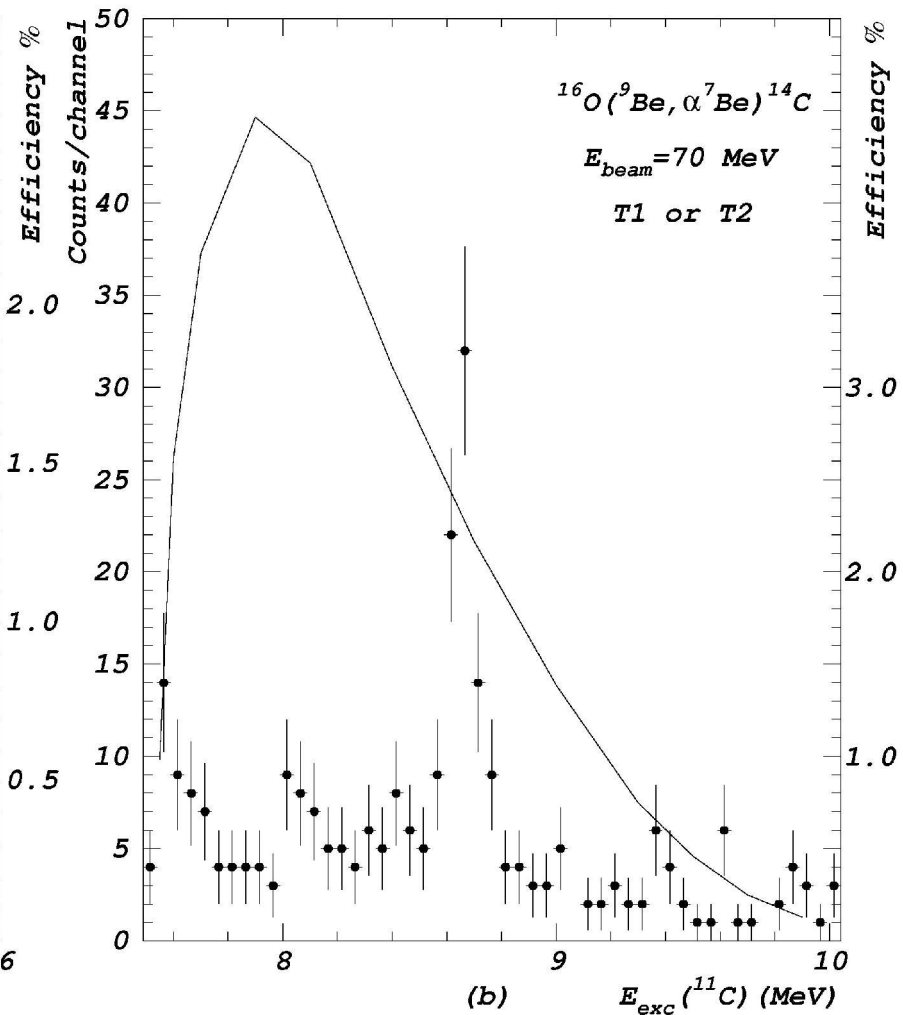
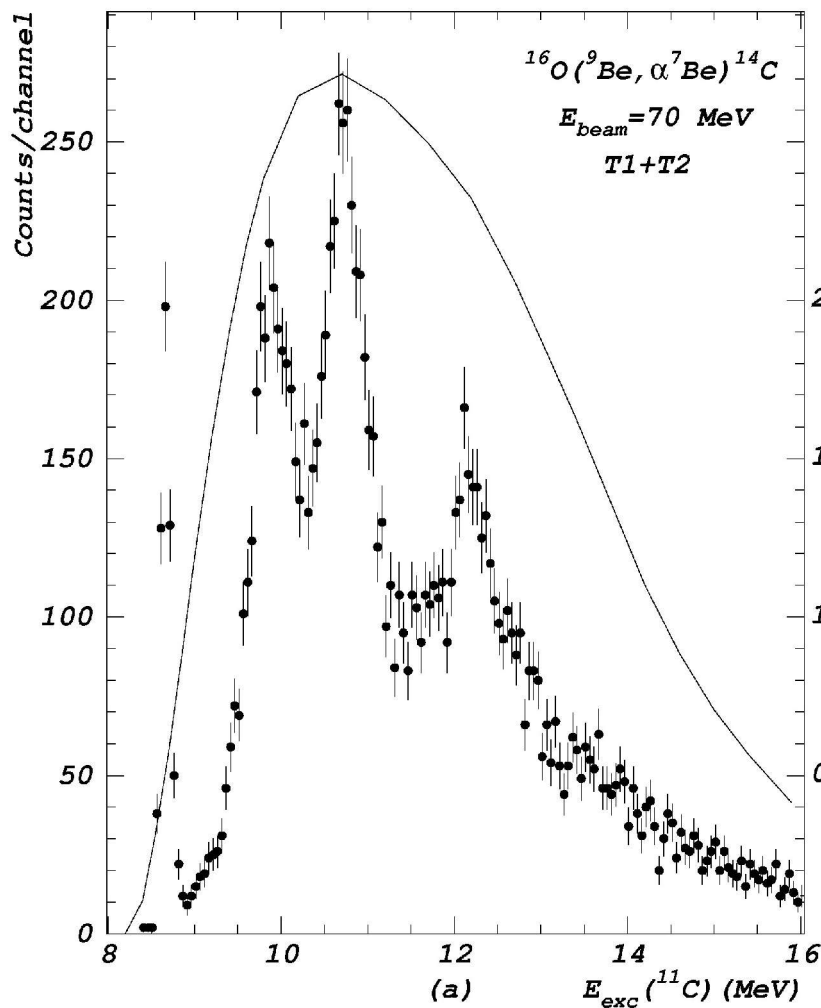
RESULTS: ^{11}C



- total energy spectra from 70 MeV data: peak at 55.4 MeV, resolution 1.3 MeV
- contributions from the ^7Be g.s. and the 1st excited state (429 keV) unresolved



- ^{11}C excitation energy reconstructed from the relative velocity of the fragments
- no contributions from the $^{18}\text{O} \rightarrow \alpha + ^{14}\text{C}$ and $^{21}\text{Ne} \rightarrow ^7\text{Be} + ^{14}\text{C}$ decays
- detection efficiency calculations performed using Monte Carlo simulations
- uncertainty in the excitation energy 100 keV, resolution 200-300 keV
- data show evidence for only $\alpha + ^7\text{Be}(\text{gs})$ decay, $E_{\text{thrs}} = 7.543 \text{ MeV}$



- reaction cross section decreases rapidly with increasing $^{11}\text{C}^*$ emission angle =>
 main reaction mechanism was **two-proton pickup to ^9Be**

^{11}C excited states decaying into $\alpha+^7\text{Be}(\text{gs})$

Present	Ajzenberg-Selove, NPA506(1990)		
	8.1045	11 eV	$3/2^-$
	8.420	15 eV	$5/2^-$
8.65	8.655	5 keV	$7/2^+$
	8.699	15 keV	$5/2^+$
	9.20	500	$5/2^+$
	9.65	210	$(3/2^-)$
9.85	9.78	240	$(5/2^-)$
	9.97	120	$(7/2^-)$
	10.083	230	$7/2^+$
10.7	10.679	200	$9/2^+$
	11.03	300	
	11.44	360	
12.1	12.16	270	$T=3/2$
	12.4	1-2 MeV	
	12.51	490	$1/2^-; 3/2$
(12.6)	12.65	360	$(7/2^+)$
	(13.01)		
	13.33	270	
(13.4)	13.4	1100	

$^{11}\text{C}^*$ decays threshold (MeV)

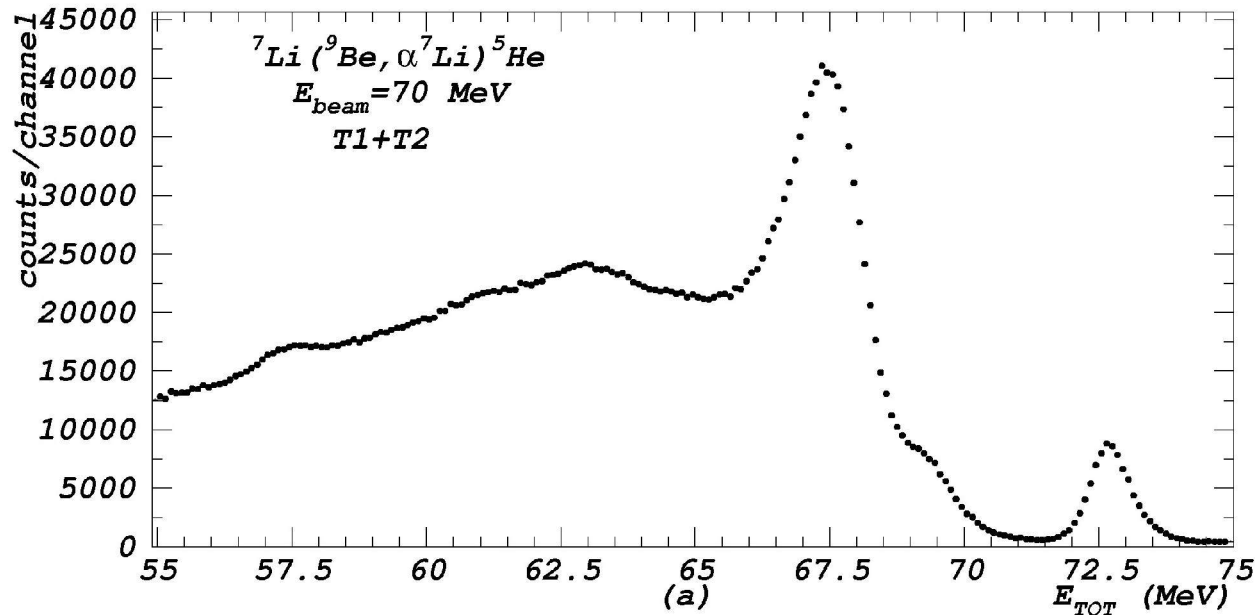
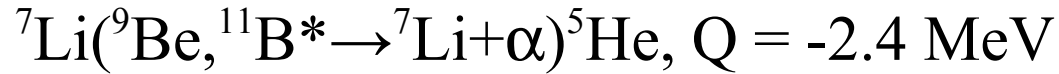
$\alpha+^7\text{Be}$	7.543
$p+^{10}\text{B}$	8.6896
$^3\text{He}+2\alpha$	9.131
$^3\text{He}+^8\text{Be}$	9.223
$n+^{10}\text{C}$	13.120

- both data sets, taken at $E_{\text{beam}}=70$
 and 55 MeV, give the same states

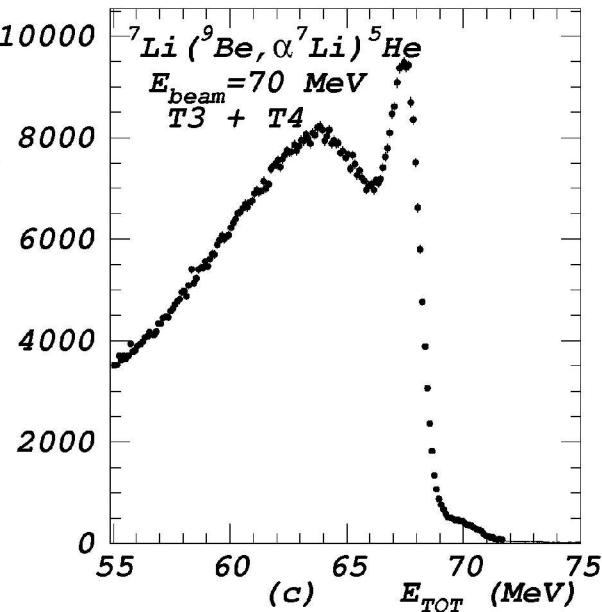
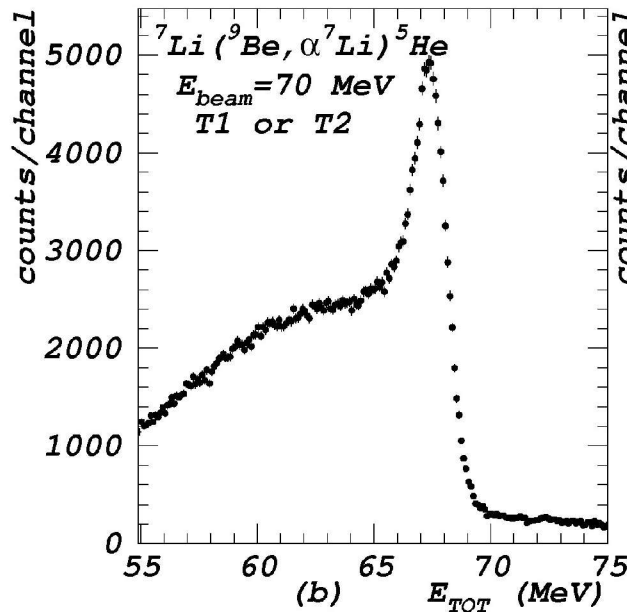
- the first direct observation of
 α -decay for states above 9 MeV

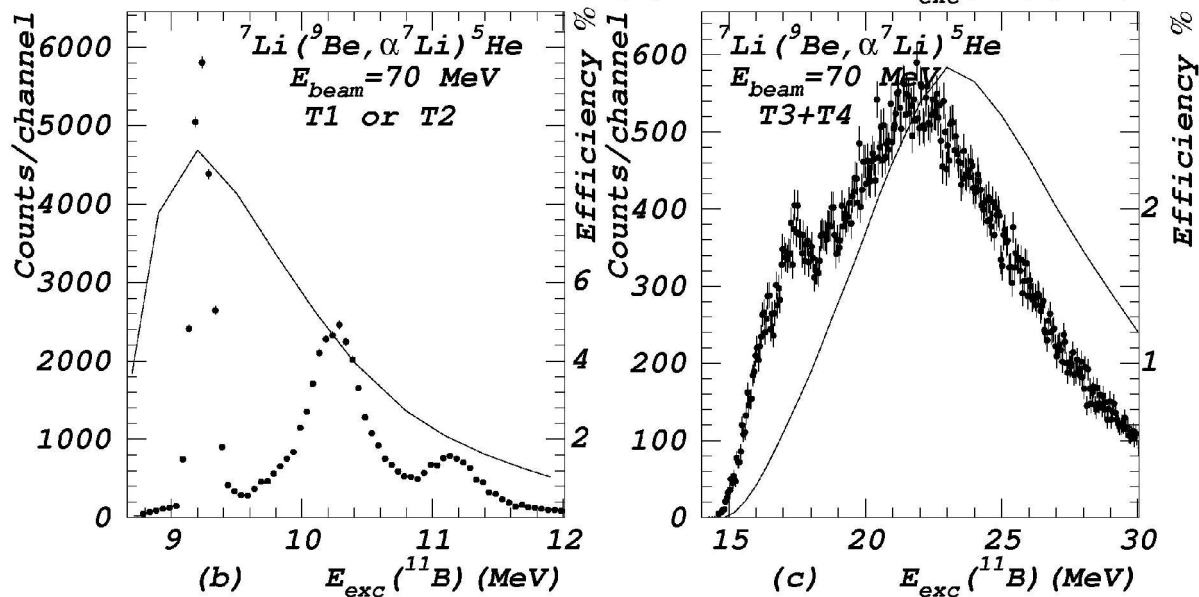
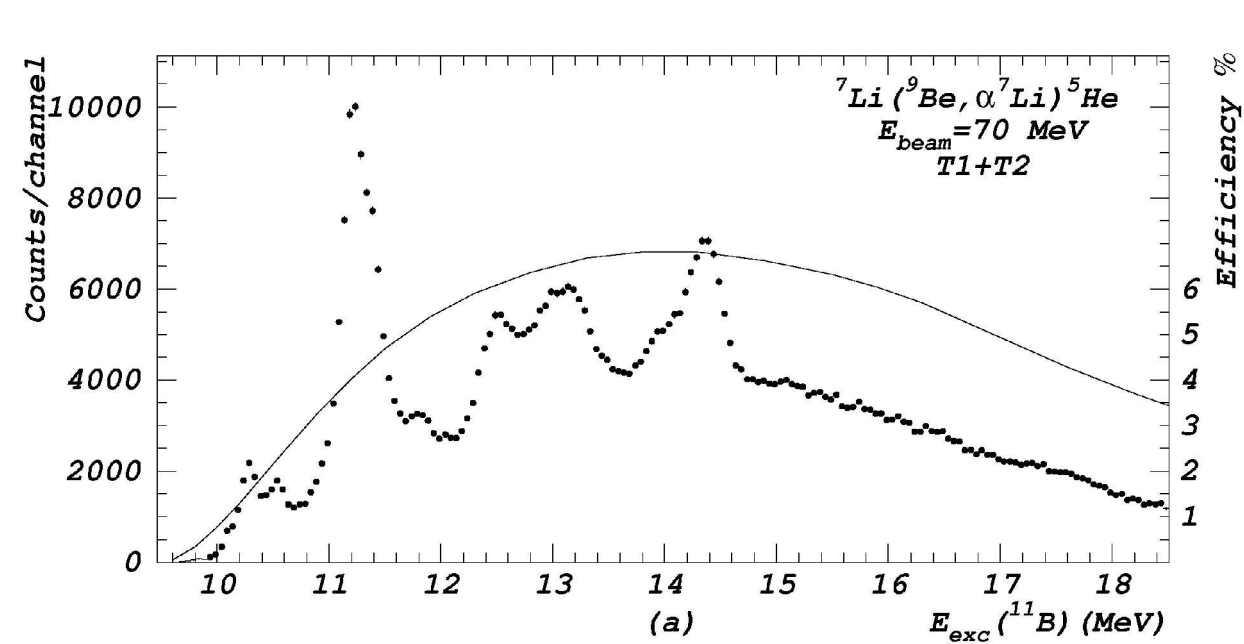
- observed strong α -decay of the
 12.1 MeV state which is proposed
 to be the isobaric analog of the
 ^{11}Be ground state

RESULTS:¹¹B



- total energy spectra from 70 MeV data, peak at 67.5 MeV, resolution 2MeV
- width of the ⁵He gs 600keV
- contributions from the ⁷Li gs and the 1st excited state (478 keV) unresolved





- no evidence for the $^{12}\text{B} \rightarrow ^7\text{Li} + ^5\text{He}$ decay, $^9\text{Be} \rightarrow \alpha + ^5\text{He}$ decay observed only in T3+T4 data (its contribution removed from the spectrum)
- uncertainty in the excitation energy is 100 keV, resolution 200 – 300 keV
- data give evidence for only $^{11}\text{B} \rightarrow \alpha + ^7\text{Li}(\text{gs})$ decay, $E_{\text{thrs}} = 8.664 \text{ MeV}$
- analysis of the angular distributions suggests **neutron pickup from ^7Li to ^9Be** , small contribution of the α -transfer from ^9Be to ^7Li possible at larger $^{11}\text{B}^*$ angles

- observed $\alpha + ^7\text{Li}(\text{gs})$ resonances extend the ^{11}B excitation energy range for this decay channel ; the same states observed at $E_{\text{beam}} = 70$ and 55 MeV

Present Ajzenberg-Selove,NPA506(1990)

^{11}B excited states decaying into $\alpha+^7\text{Li}(\text{gs})$

	8.9202	4.37 eV	$5/2^-$
9.2	9.1850	2 eV	$7/2^+$
	9.2744	4 keV	$5/2^+$
	9.82		$(1/2^+)$
	9.876	110 keV	$3/2^+$
10.3	10.26	150	$3/2^-$
	10.33	110	$5/2^-$
10.55	10.597	100	$7/2^+$
	10.96	4500	$5/2^-$
11.2	11.265	110	$9/2^+$
(11.4)	11.444	103	
	11.6	170	$5/2^+$
11.8	11.886	200	$5/2^-$
	12.0	1000	$7/2^+$
12.5	12.557	210	$1/2^+; T=3/2$
(13.0)	12.916	200	$1/2^-; 3/2$
13.1	13.137	426	$9/2^-$
	13.16	430	$(5/2, 7/2)^+$
(14.0)	14.04	500	$11/2^+$
14.35	14.34	254	$5/2^+; 3/2$
	14.565	30	
	15.29	250	$(3/2, 5/2, 7/2)^+; 3/2$
	16.437	30	$T=3/2$
	17.33	1000	
17.4	17.43	100	$T=3/2$
	18.0	870	$T=3/2$
(18.6)	18.37	260	$(1/2, 3/2, 5/2)^+$

$^{11}\text{B}^*$ decays threshold (MeV)

$\alpha+^7\text{Li}$ 8.664

$t+2\alpha$ 11.131

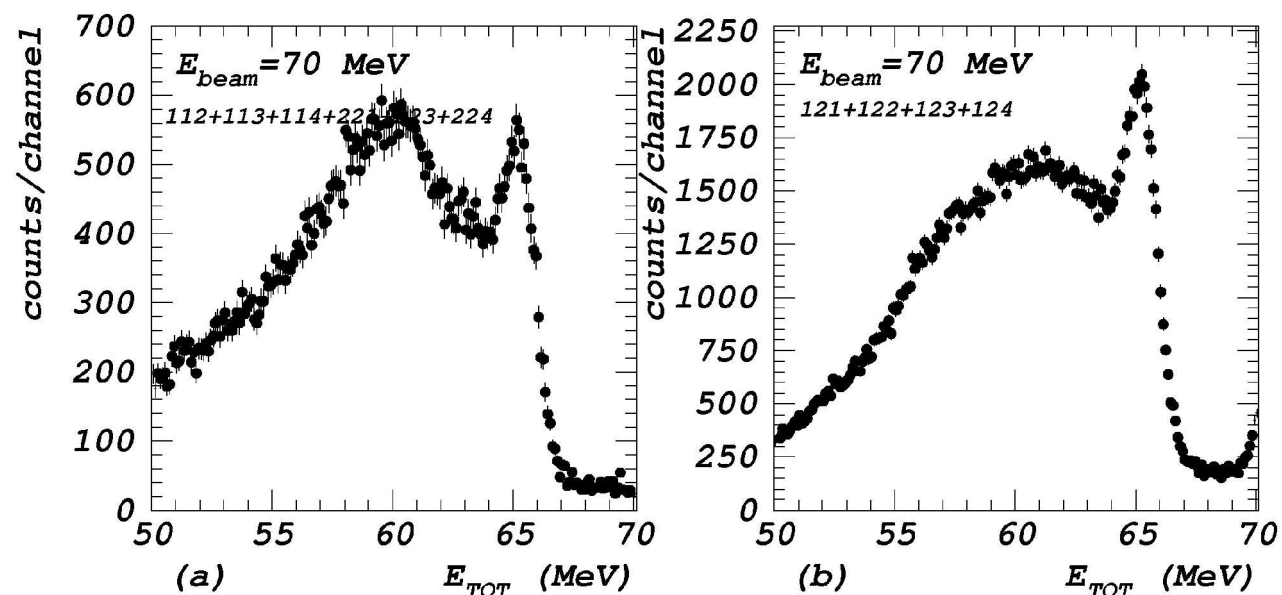
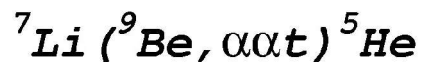
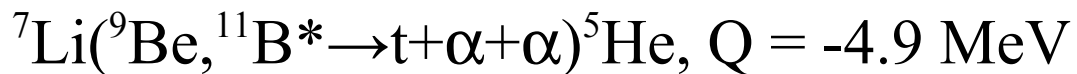
$t+^8\text{Be}$ 11.223

$p+^{10}\text{Be}$ 11.228

$n+^{10}\text{B}$ 11.454

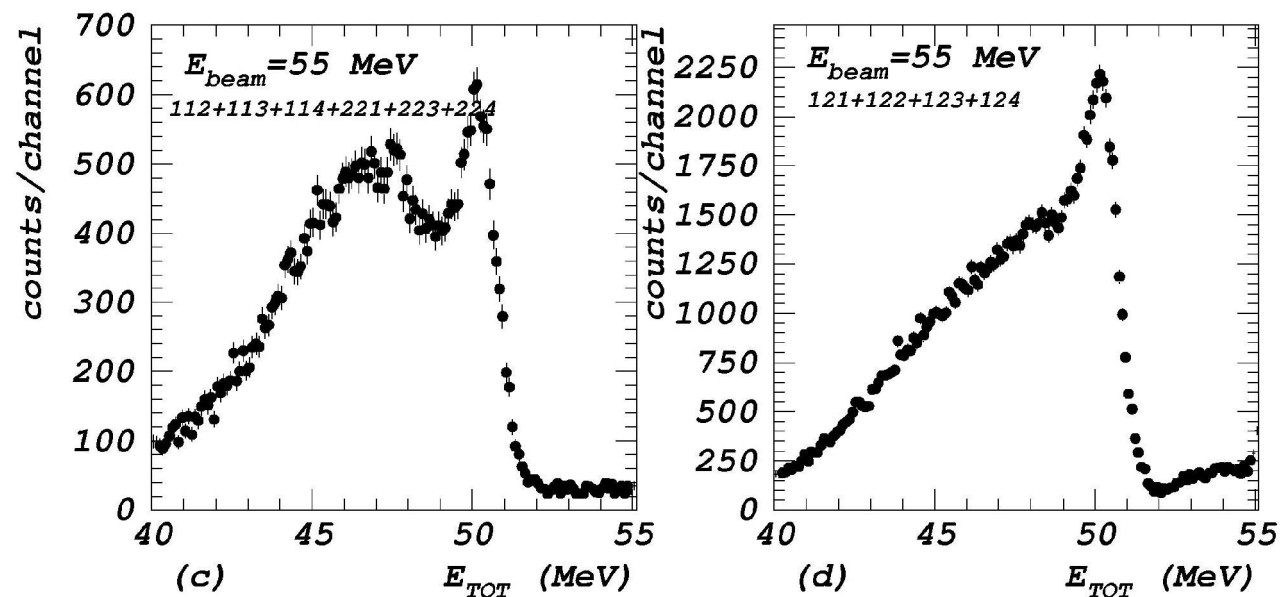
$d+^9\text{Be}$ 15.815

- four states observed here ($T=1/2$)
coincide with states proposed to be
the isobaric analogue states of the
 ^{11}Be states ($T=3/2$)



- total energy spectra at
 $E_{\text{beam}} = 70$ and 55 MeV

- peaks at 65.1 and 50.1
MeV, resolution 1.5 -2.0
MeV



- similar spectra for other
telescope combinations

- reaction identification: 3 detected particles of 4 in the exit channel

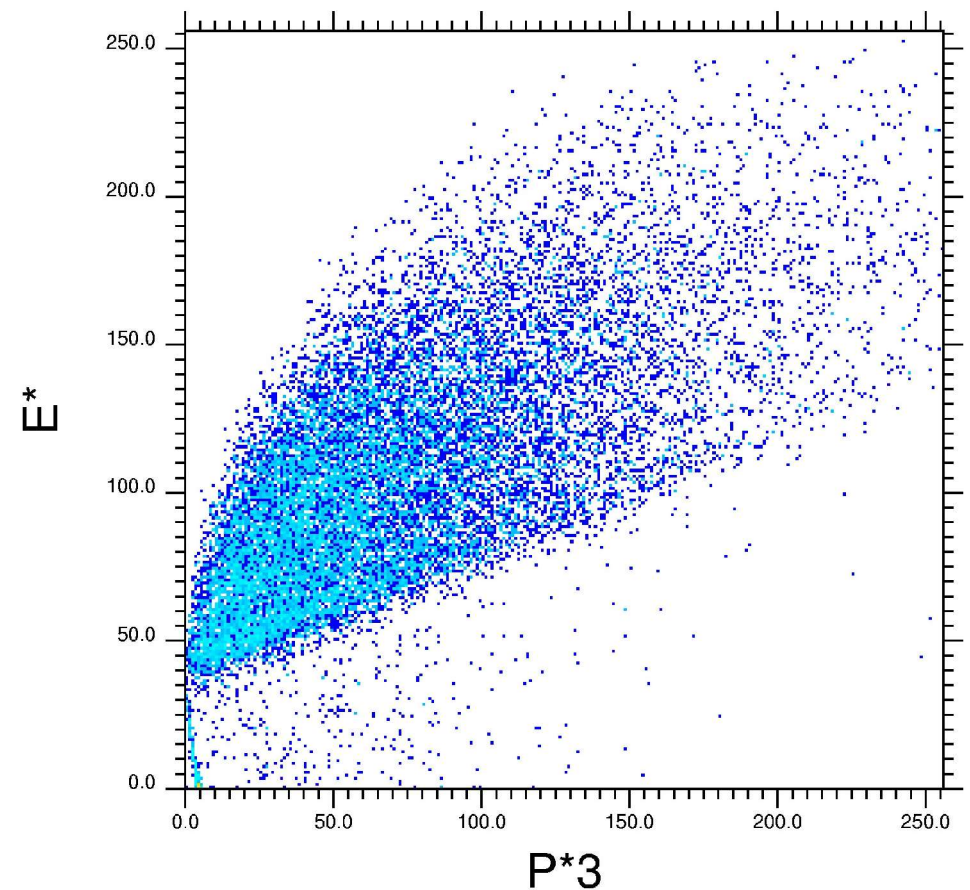
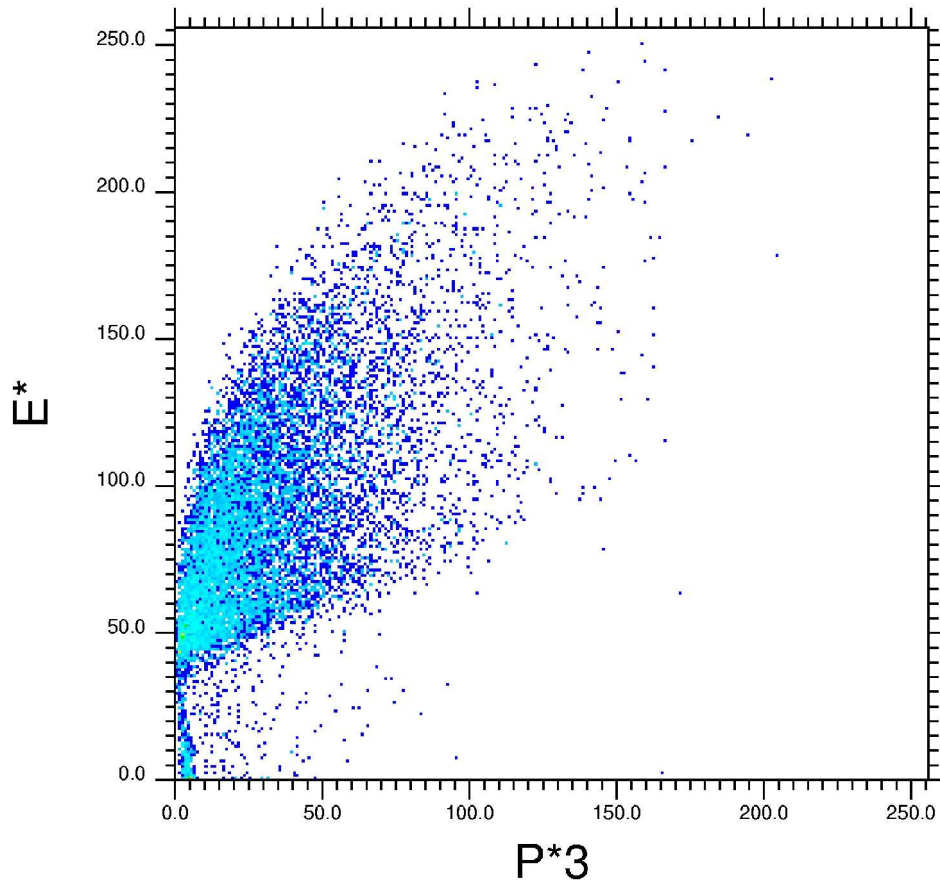
$$\tilde{P} = [\vec{p}_{beam} - \vec{p}_1 - \vec{p}_2 - \vec{p}_3]^2 / (2 \times amu)$$

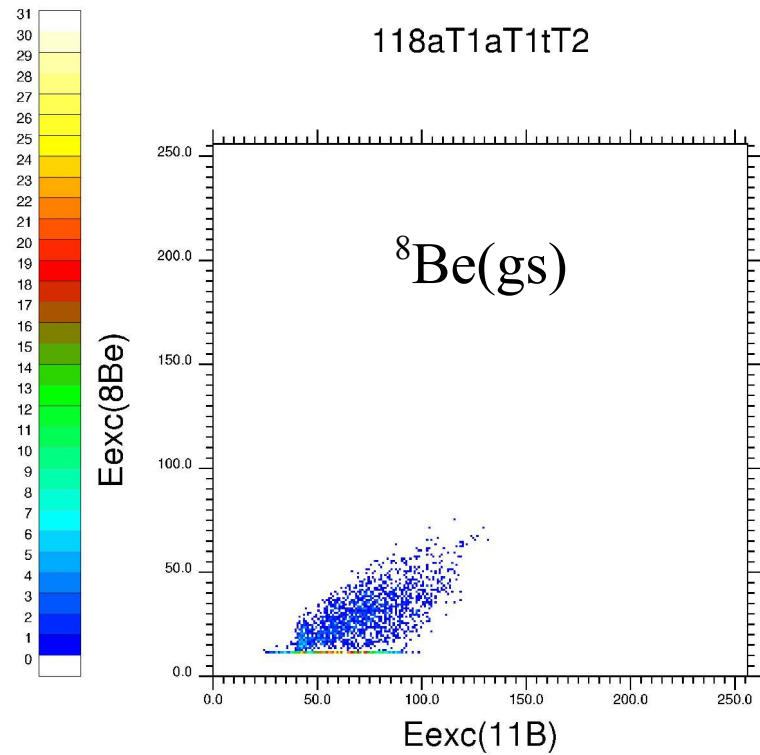
$$\tilde{E} = E_{beam} - E_1 - E_2 - E_3$$

$$\tilde{E} = \tilde{P} / A_{recoil} - Q$$

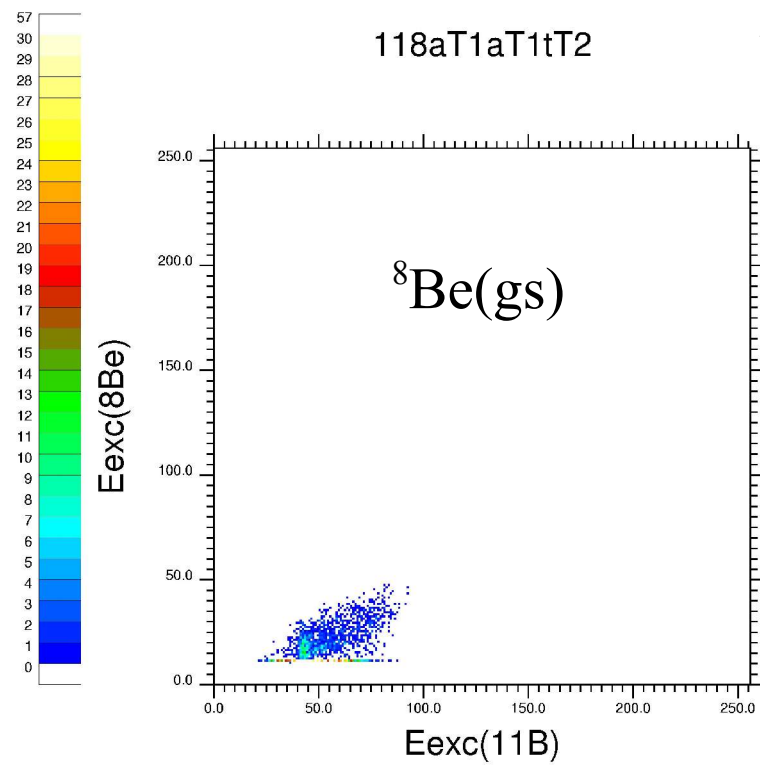
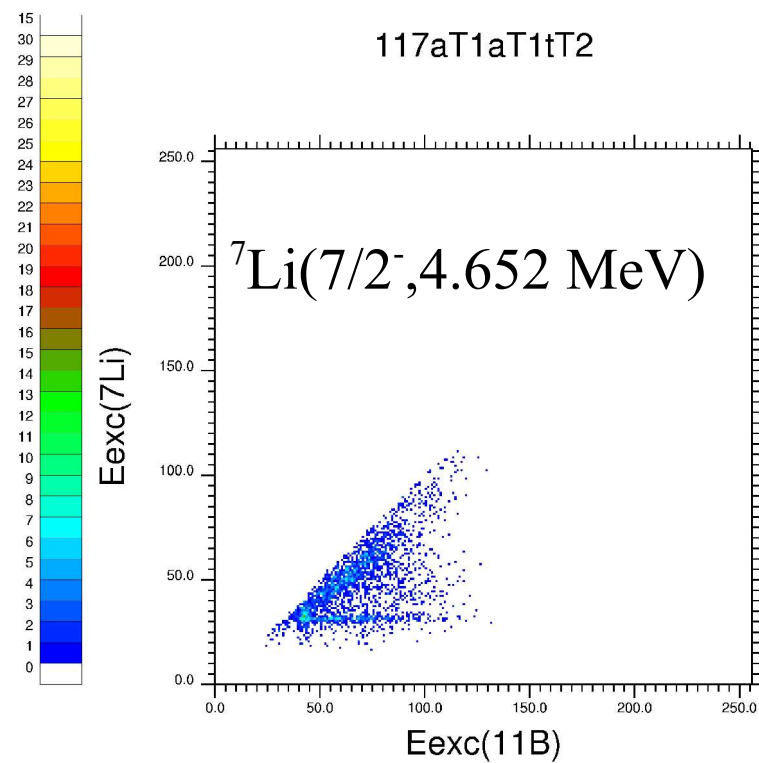
PEaT1aT2tT1

PEaT2aT3tT4



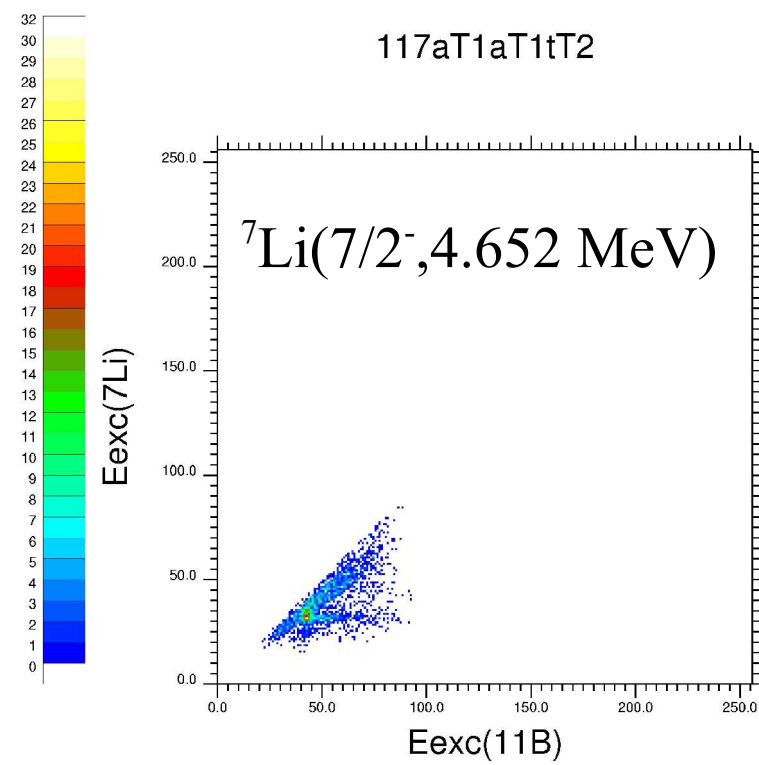


70 MeV

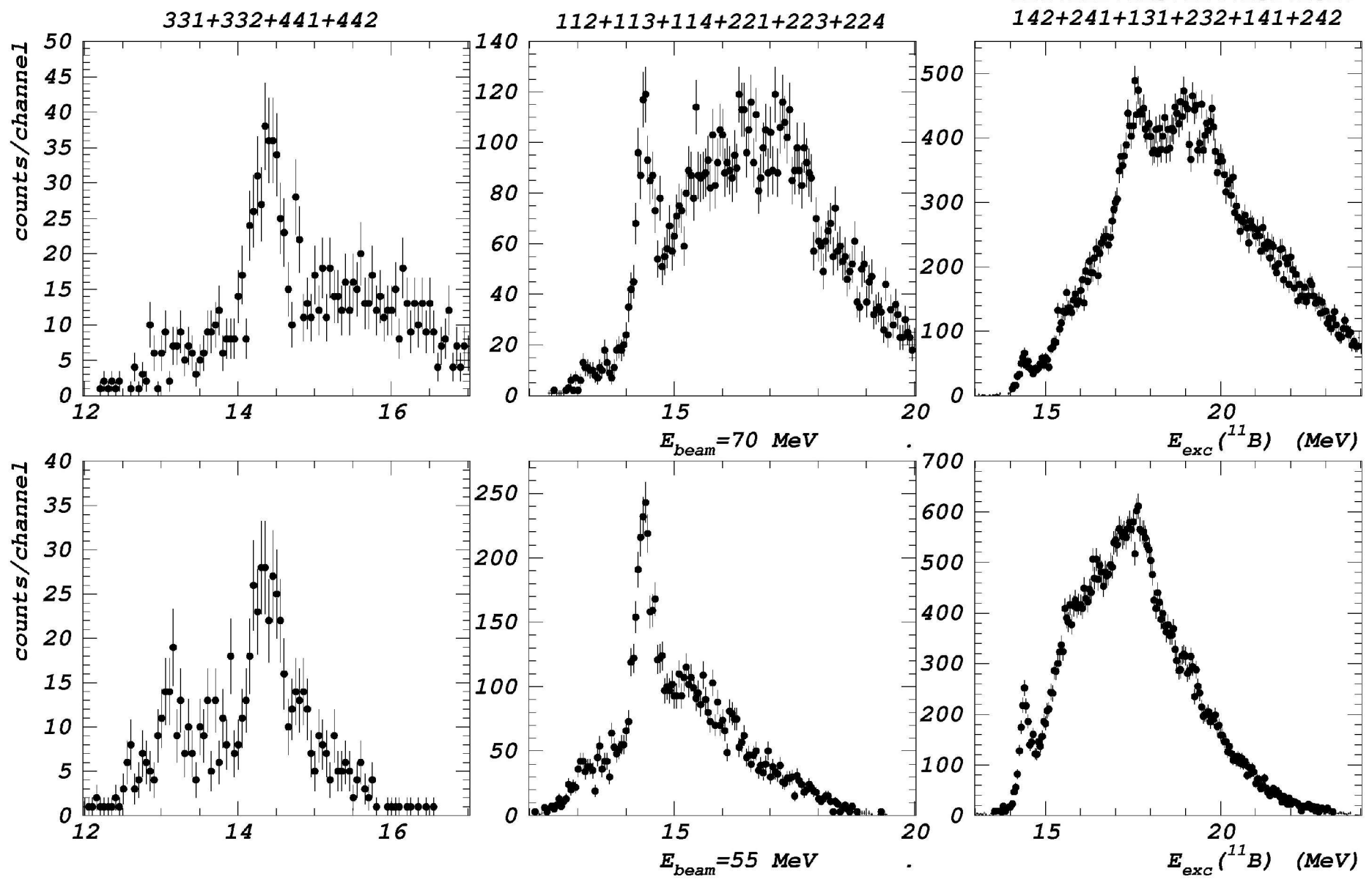
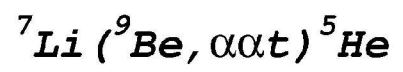


Dalitz plot

55 MeV



- ^{11}B excitation energy spectra reconstructed from the energies and momenta of 3 detected particles: peaks at 13.1, 14.4 and 17.5 MeV
- resolution 250-350 keV, uncertainty 150 keV



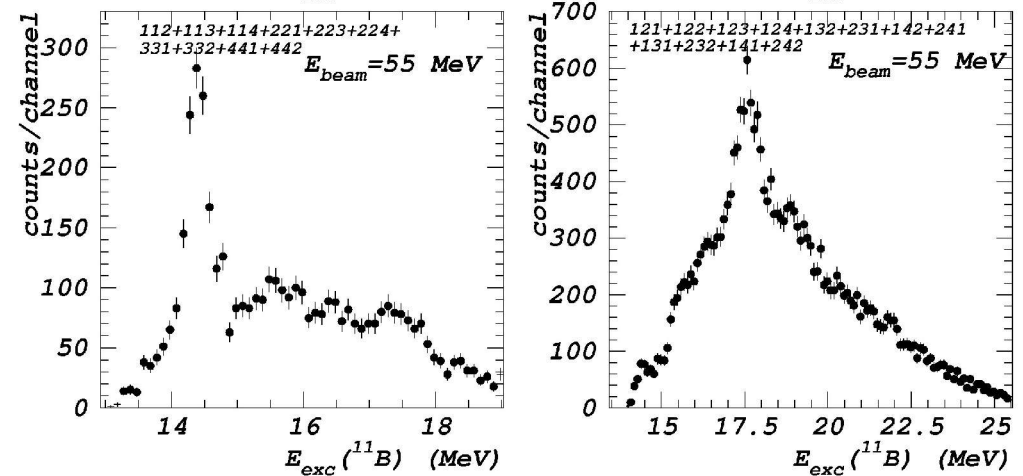
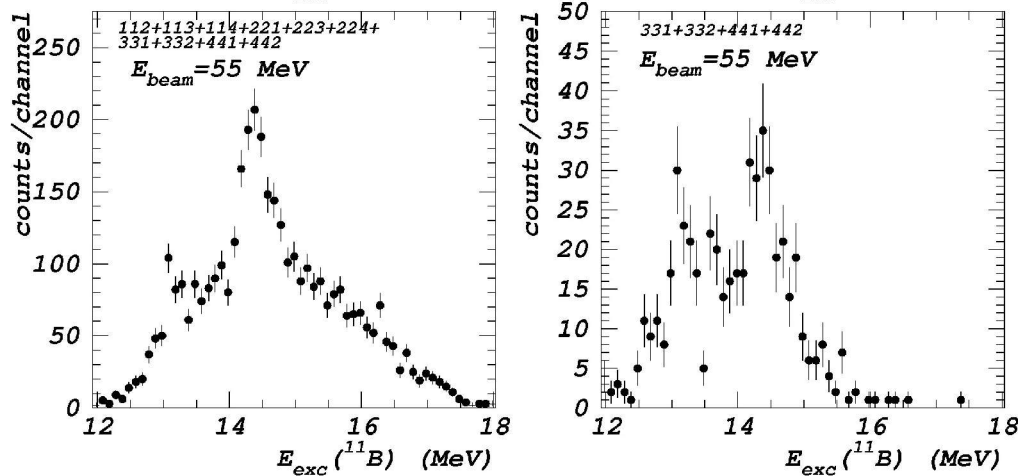
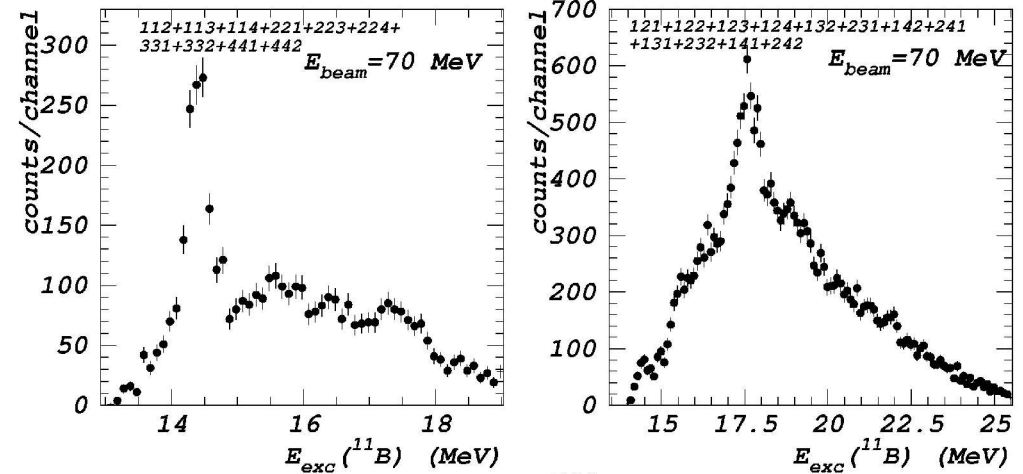
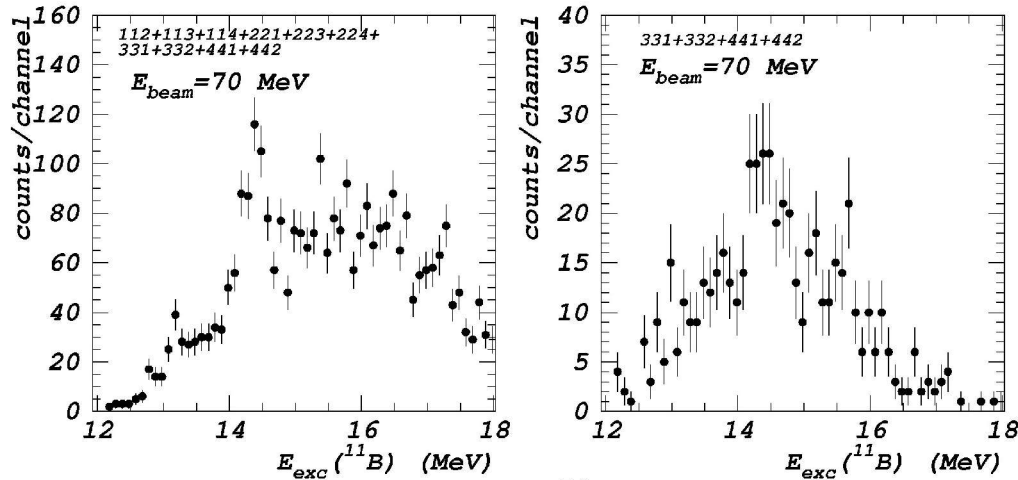
- all possible 2- and 3-body decays were reconstructed and it is clear that there is no contribution in presented spectra from any other decay process

$^{11}\text{B}^* \rightarrow t + ^8\text{Be}(\text{gs})$ decay
peaks at 13.1 and 14.4 MeV

$^{11}\text{B}^* \rightarrow \alpha + ^7\text{Li}^*(4.652 \text{ MeV})$ decay
peaks at 14.4 and 17.5 MeV

$^7\text{Li} (^9\text{Be}, t ^8\text{Be}) ^5\text{He}$

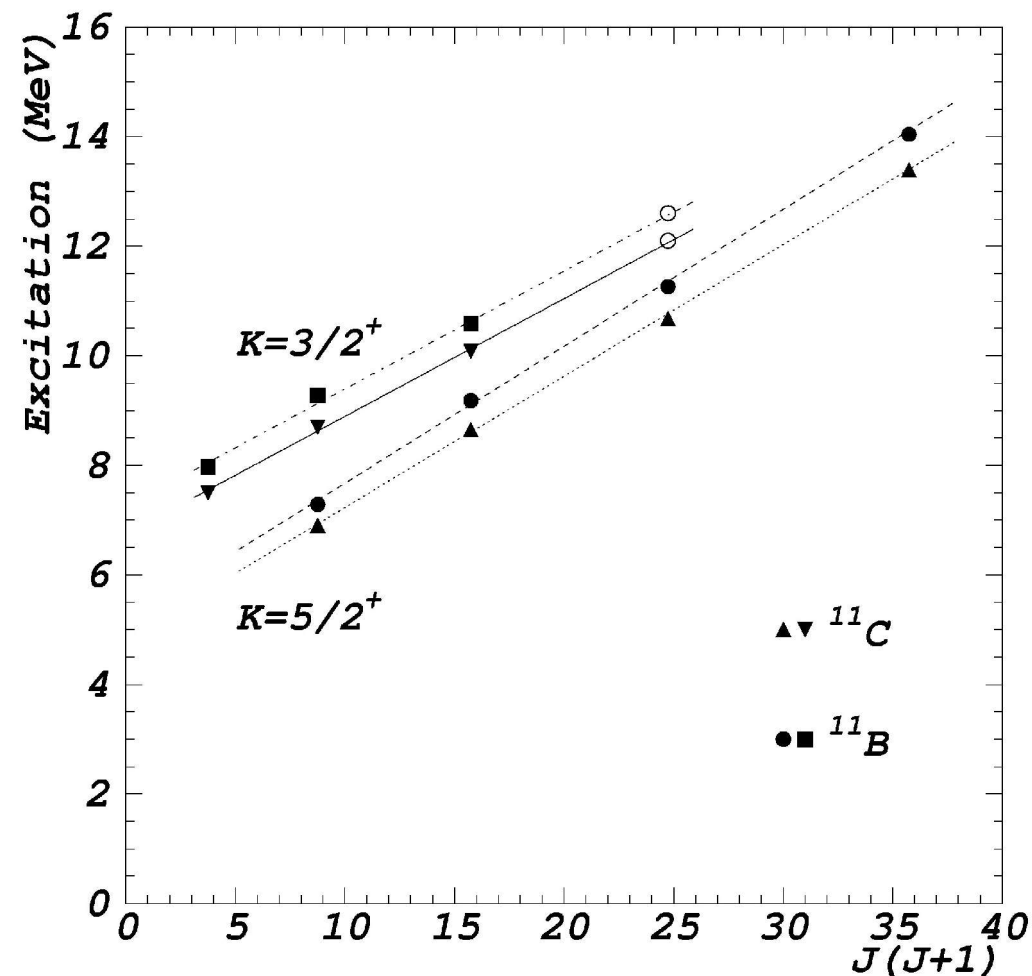
$^7\text{Li} (^9\text{Be}, \alpha ^7\text{Li}^* (7/2^-)) ^5\text{He}$



- these results are the first direct evidence for $^{11}\text{B}^*$ decays into 3 particles

COMMON FEATURES OF THE ^{11}B AND ^{11}C EXCITED STATES

- the observed ^{11}B states at 12.5, 12.9, 14.4 and 17.5 and ^{11}C state at 12.1 coincide with proposed $T=3/2$ states (isobaric analogue states of ^{11}Be)
- these states may have large isospin mixing or may be the new states which have a genuine $T=1/2$ character and may be linked to rotational bands



^{11}B :

K=5/2⁺: 7.286 9.185 11.265 14.04 MeV
rotational parameter $\hbar^2/2I = 0.25$ MeV

K=3/2⁺: 7.978 9.274 10.597 (12.5)
rotational parameter $\hbar^2/2I = 0.215$ MeV

^{11}C :

K=5/2⁺: 6.905 8.655 10.679 13.4

rotational parameter $\hbar^2/2I = 0.24$ MeV

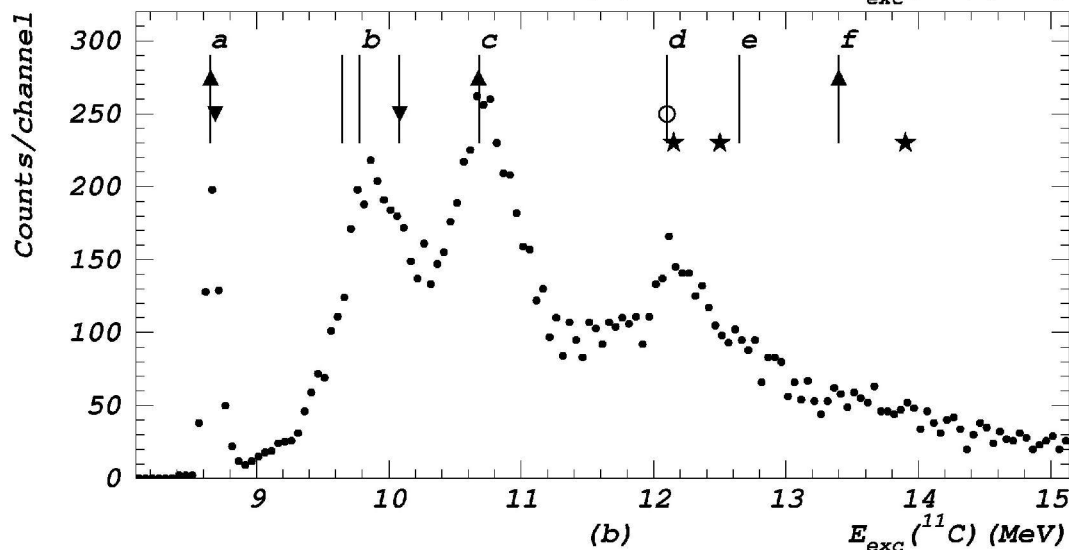
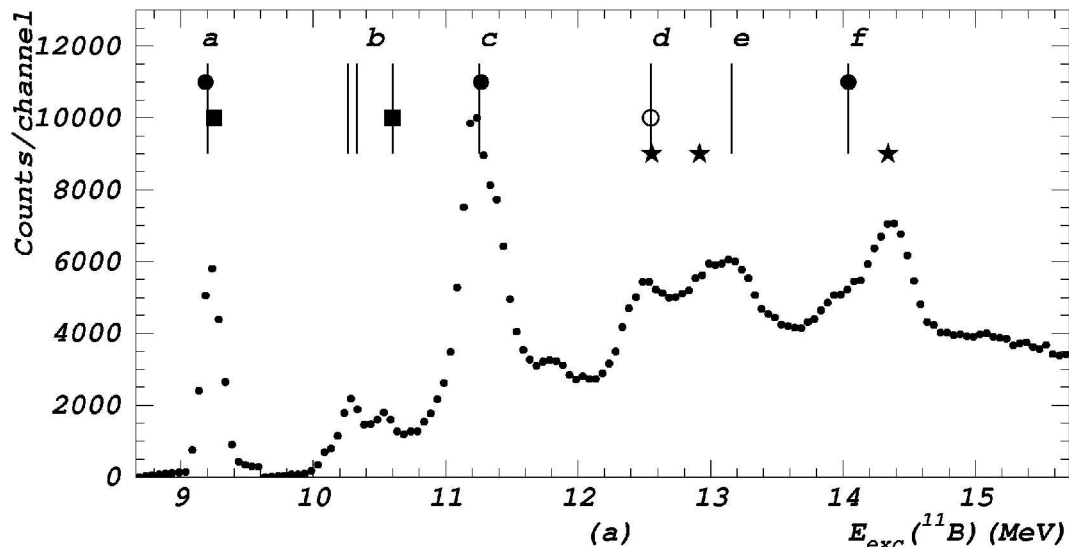
K=3/2⁺: 7.499 8.699 10.083 (12.1)

rotational parameter $\hbar^2/2I = 0.215$ MeV

=> very deformed structure

-determination of the spins and parities of the 12.5 and 12.1 MeV states in ^{11}B and ^{11}C is required

- interesting feature of the present spectra: we observe the same series of excited states at the lower excitations in both nuclei
- all states observed in ^{11}C appear also as strong resonances in ^{11}B



- these strongly excited states observed in α -decay of both nuclei **should have the same structure**

- observed strong $\alpha+{}^7\text{Li}({}^7\text{Be})$ decay of these mirror states produced in the two-nucleon transfer reactions onto ${}^9\text{Be}$ and known $\alpha+t({}^3\text{He})$ cluster structure of ${}^7\text{Li}({}^7\text{Be})$ as well as $2\alpha+t$ decay of ${}^{11}\text{B}$ states, suggest **$2\alpha+t({}^3\text{He})$ 3-centre cluster structure of the ${}^{11}\text{B}({}^{11}\text{C})$ excited states**

SUMMARY

- performed measurements provide evidence for $\alpha+{}^7\text{Be}(\text{gs})$ and $\alpha+{}^7\text{Li}(\text{gs})$, $\alpha+{}^7\text{Li}^*(7/2^-, 4.652 \text{ MeV})$, $t+{}^8\text{Be}(\text{gs})$ decays of excited states in ${}^{11}\text{C}$ and ${}^{11}\text{B}$
- the nature of the reaction processes, two-nucleon transfer onto the $2\alpha+n$ nucleus ${}^9\text{Be}$, the α -decay of excited states at excitations where various decay channels are open and known $\alpha+t({}^3\text{He})$ structure of ${}^7\text{Li}({}^7\text{Be})$, as well as observed ${}^{11}\text{B}$ decays into $2\alpha+t$, indicate that these states correspond to the **three-centre $2\alpha+t({}^3\text{He})$ cluster structure**
- this cluster structure appears to be more prominent in the **positive-parity states where two rotational bands ($K=5/2^+$ and $3/2^+$)** corresponding to very deformed structure are suggested
- the observed structure is probably **oblate** in character
- indications for **mixed isospin** of some $T=3/2$ states were found
- present measurements did not provide information on the spin and parity of these states which is crucial step to understand structure of the observed states
- measurements capable of determining these information have been proposed
- the existing theoretical calculations have not examined 3-centre systems where are holes exchanged between α -particles nor the rotational structures of the proposed 3-centre configurations and such calculations would be extremely useful